## Exercises with complex numbers

Laboratory 3

## Problem 1

Find the magnitude of the following numbers
A. $1+2 \mathrm{i}$
B. $20+13 \mathrm{i}$
C. $20 e^{140 i}$

Problem 2 Write the following numbers in the form $r e^{i \theta}$
A. $1+2 \mathrm{i}$
B. $20+13 \mathrm{i}$
C. $20+140 \mathrm{i}$

Problem 3 Write the following numbers in the form $a+i b$
A. $1 e^{2 i}$
B. $3 e^{\pi i}$
C. $2 e^{\frac{2 \pi}{3} i}$

The numbers in the exponent are in radians.
Problem 4 Find the complex conjugate of
A. $1+2 \mathrm{i}$
B. $20+13 \mathrm{i}$
C. $20 e^{140 i}$

Problem 5 Draw a sketch of the complex plane showing where each number in problem 3 is on that plane.

Problem 6 Perform the following calculations with $z_{1}=1+2 \mathrm{i}, z_{2}=-1+2 \mathrm{i}$, and $z_{3}=1+-2 \mathrm{i}$
A. $z_{1}+z_{2}$
B. $z_{1} * z_{2}$
C. $z_{1}^{*} * z_{2}$
D. $\frac{z_{1} * z_{2}}{z_{3}}$

Problem 7 Show
A. $\cos (i z)=\cosh (i z)$
B. $\sin (i z)=\sinh (i z)$

